Name: \_\_\_\_\_

Directions: Work only on this sheet (on both sides, if needed); do not turn in any supplementary sheets of paper. There is actually plenty of room for your answers, as long as you organize yourself BEFORE starting writing.

**AT THE END OF THE EXAM:** E-mail me your code, in a single file named **ID1.ID2...R**, where the ID values are the student ID numbers of the members of your group (only those present, of course).

Suppose we sample q people at random from a population consisting of m individuals, numbered 1,...,m. There are three subpopulations: Those numbered 1,...,c; those numbered c+1,...,c+d, and those numbered c+d+1,...,m. Let X, Y and Z denote the numbers of people who fall into the three subpopulations.

- (a) () Suppose the sampling is with replacement. Find the exact value of  $p_{X,Y,Z}(i, j, k)$ . Express your answer as an R function, rplcsamp(m,q,c,d,i,j,k).
- (b) () Same as (a), except that sampling is without replacement. Your R function will be norplcsamp(m,q,c,d,i,j,k).
- (c) () Same as (b), except that the probability is found via simulation. The call is simnorplcsamp(m,q,c,d,i,j,k,nreps), with a default value of 10000 for nreps.

Do NOT include any error-checking code.