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Statistical Cinderella: Parallel Computation for the Rest of Us

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R/Finance 2018 Chicago, IL, USA, 1 June, 2018

These slides will be available at http://heather.cs.ucdavis.edu/rifinance2018.pdf

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Statistical Cinderella: Parallel Computation for the Rest of Us

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- "Everyone has opinions."
- I'll present mine.
- Dissent is encouraged. :-)

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The Drivers and Their Result

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The Drivers and Their Result

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• Parallel hardware for the masses:

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The Drivers and Their Result

- Parallel hardware for the masses:
 - 4 cores standard, 16 not too expensive

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• Big Data

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 - Whatever that is.

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"I've got the hardware and I've got the data need so I should be all set to do parallel computation in R on the data."

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Result: Users believe,

"I've got the hardware and I've got the data need so I should be all set to do parallel computation in R on the data."

But this "rule" is "honored in the breach," as the Brits say.

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Not So Simple

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Not So Simple

• "Embarrassingly parallel" (EP) vs. non-EP algorithms.

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- "Embarrassingly parallel" (EP) vs. non-EP algorithms.
- EP: Problem can be easily broken down in independent tasks, with easy combining.

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 - Contention for I/O ports.

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 - OS/R limits on number of sockets (network connections).

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 - OS/R limits on number of sockets (network connections).
 - Serialization.

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Wish List

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Wish List

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• Ability to run on various types of hardware — from R.

Wish List

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- Ease of use for the non-cognoscenti.

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- Ability to run on various types of hardware from R.
- Ease of use for the non-cognoscenti.
- Parameters to tweak for the experts or the daring.

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Outline of My Remarks

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Outline of My Remarks

• Overview of existing parallel computation options for R users.

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- Overview of existing parallel computation options for R users.
 - Level in terms of abstraction, i.e. high-level constructs.

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- Overview of existing parallel computation options for R users.
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 - Level in terms of tech sophistication needed.

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"Help, I'm in over my head here!" – a prominent R developer, entering the parallel comp. world.

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• "Cinderellas": Many users are being overlooked.

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 - Not enough automatic, tranparent parallelism.

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 - Not enough for quants, e.g. for time series methods.

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- "Cinderellas": Many users are being overlooked.
 - Not enough automatic, tranparent parallelism.
 - Not enough for quants, e.g. for time series methods.
- Well then, what can be done?

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Available Software

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Available Software

software	abstr. level	handle non-EP	sophis. level
C++/OpenMP	low	very good	very high
C++/GPU	low	poor	super high
RcppPar. pkg	low	good	very high
parallel pkg	medium	medium	medium
Rdsm pkg	low	good	high
Spark/R pkgs	medium	poor	high
Rmpi pkg	low	good	high
foreach pkg	medium	poor	medium
partools pkg	medium	good	high medium
future pkg	medium	medium	high medium

(OpenMP: standard library for parallelizing on multicore)

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The Takeaways

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• R has an impressive array of parallel software tools available.

The Takeaways

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• R has an impressive array of parallel software tools available. Better than Python!

The Takeaways

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- R has an impressive array of parallel software tools available. Better than Python!
- However, all of those tools require a fair amount of programming sophistication to use.

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Speciality Packages with Transparent Parallelism

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• Using OpenMP, e.g. xgboost, recosystem.

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- Using OpenMP, e.g. xgboost, recosystem.
- Using GPU, e.g. gmatrix (not active?).

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- Using OpenMP, e.g. xgboost, recosystem.
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- Even though transparent to the user in principle, may still need expertise in hardware/systems to make it run well.

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- Using OpenMP, e.g. xgboost, recosystem.
- Using GPU, e.g. gmatrix (not active?).
- Even though transparent to the user in principle, may still need expertise in hardware/systems to make it run well.
 E.g. choice of number of threads, memory capacity issues.

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In Other Words...

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In Other Words...

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• We need to FACE FACTS.

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Statistical Cinderella:

Parallel Computation for the Rest of Us

- We need to **FACE FACTS**.
- The days in which data scientists could rely on "black boxes" are GONE.

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Statistical Cinderella:

Parallel Computation

- We need to FACE FACTS.
- The days in which data scientists could rely on "black boxes" are GONE.
- One needs to have at least some knowledge of the innards:

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 - Machine Learning tuning parameters defaults underfit, naive grid search selection overfits.

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 - For effective parallel computation, one must be adept at coding and at software "tuning parameters," e.g. number of threads.

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 - Machine Learning tuning parameters defaults underfit, naive grid search selection overfits.
 - For effective parallel computation, one must be adept at coding and at software "tuning parameters," e.g. number of threads.
- Little or no hope for good automatic parallelism.

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Parallel Computation of Time Series Analyses

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Parallel Computation of Time Series Analyses

Now let's turn to time series.

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Now let's turn to time series. (Disclaimer: I am not an expert in time series.)

• Some parallel methods have been developed.

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Parallel Computation of Time Series Analyses

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- E.g., if large matrices are involved (say models with long memory), one can use OpenMP to parallelize matrix computations

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- E.g., if large matrices are involved (say models with long memory), one can use OpenMP to parallelize matrix computations
- In some cases one can find a clever way to parallelize a specific algorithm (F. Belletti, arXiv, 2015).

• But it's much harder than for i.i.d. models.

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Possible Obstacles

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Possible Obstacles

• Matrix addition/multiplication is EP, but inversion is not.

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- Breaking t.s. data into chunks might not be EP, due to boundary effects.

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- Parallelization based on math structures difficult to show asymptotic validity.
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- Breaking t.s. data into chunks might not be EP, due to boundary effects. E.g. computing number of consecutive periods in which value is above a threshold — could span two chunks, or even more.
- Hyndman's Rule: Any time series model eventually starts to go bad after very long lengths.

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Our partools Package

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Our partools Package

On CRAN, but go to github.com/matloff for the latest version.

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- On CRAN, but go to github.com/matloff for the latest version.
- Large variety (78+) of functions for parallel **data manipulation** and **computation**.

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- Some functions do a lot, some just a little. The latter can be combined into powerful tools, as with Unix/Linux/Mac scripting.

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- Large variety (78+) of functions for parallel **data manipulation** and **computation**.
- Some functions do a lot, some just a little. The latter can be combined into powerful tools, as with Unix/Linux/Mac scripting.
- Built on top of **parallel** pkg., plus our own MPI-like internal system.

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Themes

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Themes

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• "Leave It There" (LIT) theme: Keep data distributed as long as possible throughout an analysis session, to avoid costly communications delays.

Themes

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Themes

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- "Leave It There" (LIT) theme: Keep data distributed as long as possible throughout an analysis session, to avoid costly communications delays. Borrows distrib. object approach from Hadoop/Spark but much more flexible.
- "Software Alchemy" convert non-EP to stat. equivalent EP, thus easy parallelization.

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Possible Obstacles

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Can we extend partools to time series applications?

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Possible Obstacles

Can we extend **partools** to time series applications? Must overcome:

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Possible Obstacles

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Can we extend **partools** to time series applications? Must overcome:

- Boundary effects problems.
- SA predicated on i.i.d.

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Sample partools Session

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Sample partools Session

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• Wikipedia page-access data, Kaggle, 145063 time series of length 550.

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Sample partools Session

- Wikipedia page-access data, Kaggle, 145063 time series of length 550.
- Say we wish to run **arma()** for each page. Each is quick, but 145K of them takes some time. Say we are interested only in **ar1**.

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- Say we wish to run **arma()** for each page. Each is quick, but 145K of them takes some time. Say we are interested only in **ar1**.
- Afterward, we will perform various other operations.
- By LIT Principle, first distribute the data to the workers, then avoid collecting it back to the manager node if possible.

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Serial Version

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Serial Version

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Statistical Cinderella:

Parallel Computation

wd ← as.matrix(read.csv('train_1.csv'))
wdc ← wd[complete.cases(wd),]
armac ← function(x)
 {z ← NA; try(z ← arma(x)\$coef[1]}; z)
system.time(z ← apply(wdc,1,armac))
624.452 0.164 624.648
find the ones with weak correlation
for further analysis
wdlt05 ← wdc[z < 0.5,]
various further ops (not shown)</pre>

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Same But with partools

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The plan:

Same But with partools

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Same But with partools

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• Distribute the data and LIT. Work on it solely in distributed form as much as possible.

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Same But with partools

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Same But with partools

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The plan:

- Distribute the data and LIT. Work on it solely in distributed form as much as possible.
- Distrib. by calling **partools:::distribsplit()**, then later save using **partools:::filesave()**.
- The chunks all have the same name, in this case wdc. The manager then issues commands via clusterEvalQ(), the same command to each worker.
- At end of session, save to **partools** distributed file, **so don't need to redistribute next time.**

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Parallel Version

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Parallel Version

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Statistical Cinderella:

Parallel Computation for the Rest of

```
cls ← makeCluster(4)  # 'parallel' cluster
setclsinfo(cls)  # init 'partools'
distribsplit(cls, 'wdc')  # distrib. to workers
clusterEvalQ(cls, library(tseries))
clusterExport(cls, 'armac')
system.time(clusterEvalQ(cls,
    ar1 ← apply(wdc,1,armac)))
# 0.024 0.000 180.653
clusterEvalQ(cls, wdlt05 ← wdc[ar1 < 0.5,])  # LIT!
# various further ops (not shown)
# now save, in wdc.1, wdc.2,...
filesave(cls, 'wdc', 'wdc', 1, ', ')
```

Parallel Version

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# now save, in wdc.1, wdc.2,...
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```

The **one-time** overhead of distributing the data will continue to pay off in further analyses.

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More LIT Helpers

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More LIT Helpers

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- Can distribute the file directly, using partools:::filesplit().
 - The functions **fileread()** and **filesave()** automatically add a suffix to the name for chunk number, e.g. **wdc.1**.
 - If do need to "undistribute," **distribcat()** will do so, adding the proper header.
 - Functions such as **dwhich.min()** treat a distributed data frame as a virtual single d.f., returning row number within chunk number.
 - Etc.

Statistical Cinderella:

Parallel Computation for the Rest of Us Norm Matloff University of California at Davis

Norm Matloff University of California at Davis Software Alchemy: Parallel Computation for the Masses

Norm Matloff University of California at Davis Software Alchemy: Parallel Computation for the Masses

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Norm Matloff University of California at Davis Software Alchemy: Parallel Computation for the Masses

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Norm Matloff University of California at Davis Software Alchemy: Parallel Computation for the Masses

- I call this approach Software Alchemy (SA) (Matloff, JSS, 2016). Method independently proposed by several authors.
- Very simple idea:
 - Break the data into disjoint chunks.
 - Apply the estimator to each chunk, getting $\hat{\theta}_i$ for chunk *i*.

• Average the $\hat{\theta}_i$ to get overall $\hat{\theta}$.

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- For ML classification algs, "vote" among chunks.

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- Average the $\hat{\theta}_i$ to get overall $\hat{\theta}$.
- For ML classification algs, "vote" among chunks.
- Converts non-EP to stat. equivalent EP. Thus easy parallelization, possibly even superlinear speedup.

Norm Matloff University of California at Davis Software Alchemy: Parallel Computation for the Masses

- I call this approach Software Alchemy (SA) (Matloff, JSS, 2016). Method independently proposed by several authors.
- Very simple idea:
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 - For ML classification algs, "vote" among chunks.
- Converts non-EP to stat. equivalent EP. Thus easy parallelization, possibly even superlinear speedup.
- The partools package has a number of SA ops available.

Norm Matloff University of California at Davis

SA for Time Series

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SA for Time Series

• Not i.i.d. but stationarity and finite memory should be enough to prove that it works.

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SA for Time Series

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- Not i.i.d. but stationarity and finite memory should be enough to prove that it works.
- Should work for ARMA, ARIMA, GARCH, etc.

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SA for Time Series

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- Not i.i.d. but stationarity and finite memory should be enough to prove that it works.
- Should work for ARMA, ARIMA, GARCH, etc.
- All this should be considered preliminary.

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Example

```
Us
Norm Matloff
University of
California at
Davis
```

Statistical Cinderella:

Parallel Computation for the Rest of

```
library (TSA)
z \leftarrow garch.sim(alpha=c(.01,0.9), n=5000000)
system.time(print(garch(z)))
# Coefficient(s):
#
          a.0
                       a1
                                   b1
\# 1.001 e - 02 8.980 e - 01 3.775 e - 12
\# 13.088 0.140 13.228
cls \leftarrow makeCluster(2)
setclsinfo(cls)
distribsplit (cls, 'z')
system.time(zc2 \leftarrow clusterEvalQ(cls, garch(z)$coef))
\# 0.000 0.000 5.925
Reduce('+',zc2) / 2
                                            b1
#
              a.0
                             a1
\# 1.004293e - 028.910964e - 013.120723e - 05
```

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SA version pretty good, 2X speed with coeffs close.

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SA version pretty good, 2X speed with coeffs close. But a 4-worker run gave 0.83 for $\mathbf{a1}$, a bit further off.

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Cinderella:
Parallel
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for the Rest of
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Statistical

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SA version pretty good, 2X speed with coeffs close. But a 4-worker run gave 0.83 for $\mathbf{a1}$, a bit further off. More study needed!

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Conclusions

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No "silver bullet."

Conclusions

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Conclusions

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No "silver bullet." But the following should go a long way toward your need for parallel computation.

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Conclusions

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No "silver bullet." But the following should go a long way toward your need for parallel computation.

• "Leave it there" and distributed objects/files.

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Conclusions

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Cinderella: Parallel Computation for the Rest of Us

Statistical

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Ready for the dissent. :-)

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Statistical Cinderella: Parallel Computation for the Rest of Us

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And sorry if I have omitted your favorite software. Just let me know. :-)