

Regression Fit Diagnostics Using freqparcoord

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UCLA
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Intro to freqparcoord

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- and for regression diagnostics—our topic here.

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Example

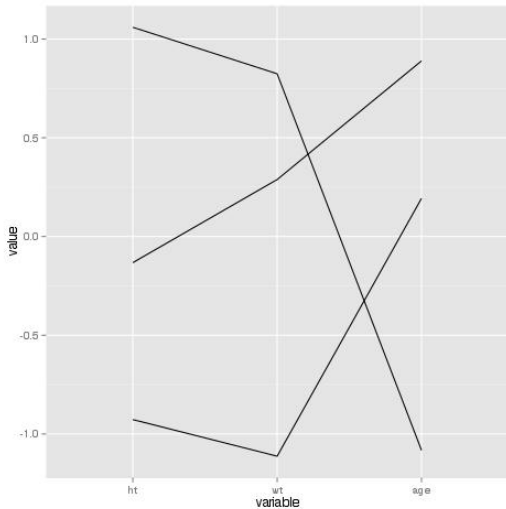
Example

Example: Height/weight/age data.

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```
> d
  ht  wt age
1 71 175 25
2 66 128 36
3 68 162 42
```



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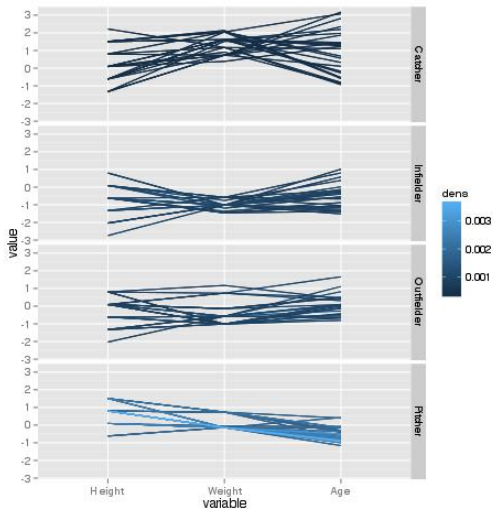
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UCLA Baseball Player Data

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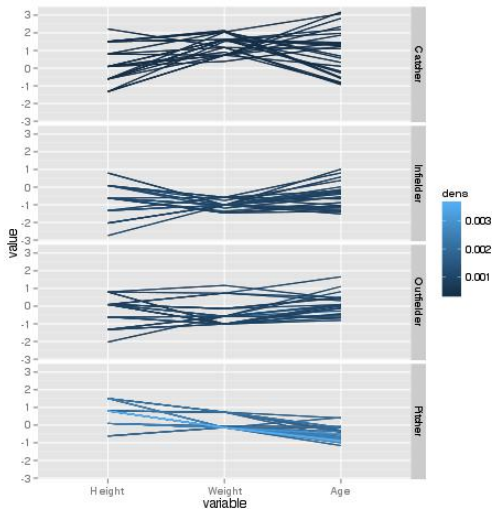
Most typical 25 points for each playing position.



- Catchers heavier, vary widely in height and age.

UCLA Baseball Player Data

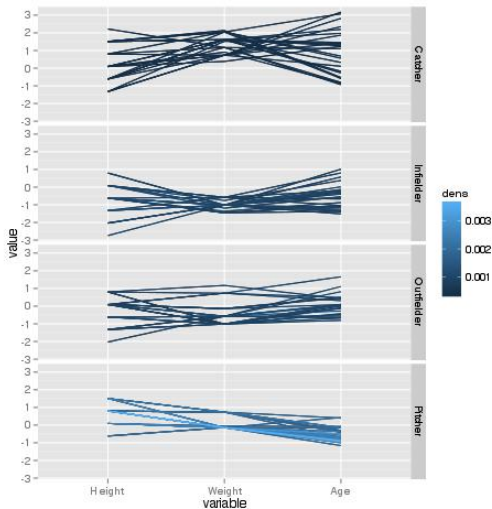
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Most typical 25 points for each playing position.



- Catchers heavier, vary widely in height and age.
- Pitchers tall, lighter, less variable in age.
- Infielders vary considerably in height but not weight.

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(Uses k-NN for nonparametric est..)

- The divergences are NOT the residuals (i.e. not actual - fitted parametric).

Application to Regression Diagnostics

Our **fregparcoord** package includes a function **regdiag()**.

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- What **regdiag()** does it look at the typical values among the most negative and most positive divergences.

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Our **freqparcoord** package includes a function **regdiag()**.

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- The divergences are NOT the residuals (i.e. not actual - fitted parametric).
- What **regdiag()** does it look at the typical values among the most negative and most positive divergences.
- In other words: **regdiag()** asks, “In what region[s] of predictor space is the fit poorer?”

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Programmers and engineers in Silicon Valley, 2000 Census, 5% PUMS.

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```
> data(prgeng) # fpc. built-in data set
> pg1 <- prgeng
> pg1$ms <- as.integer(pg1$educ == 14) # MS
> pg1$phd <- as.integer(pg1$educ == 16) # PhD
> pg1$se <- as.integer(pg1$occ==102) # s. eng
> l1 <- lm(wageinc ~ age+ms+phd+se+sex, data=pg1)
# look at 40% most neg., 40% most pos. divs.
> p <- regdiag(l1, tail=0.40)
> p # display graph
> p$paramr2 # parametric adj. R2
[1] 0.07027561
> p$nonparamr2 # nonparamr2 R2
[1] 0.1286746
```

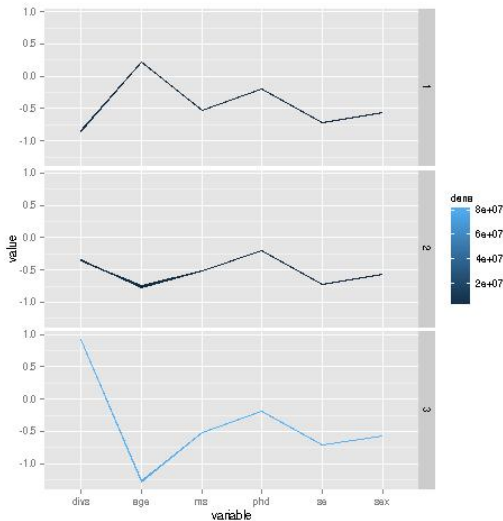
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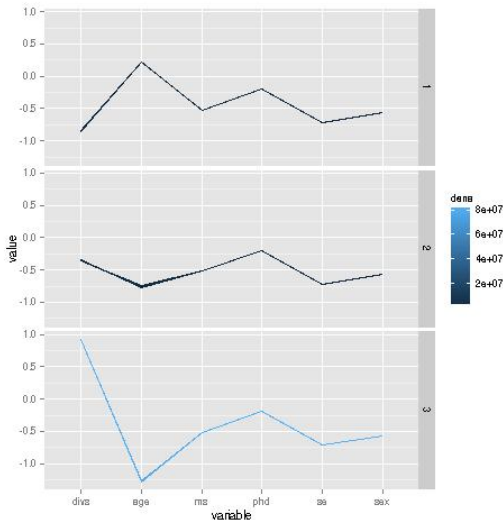
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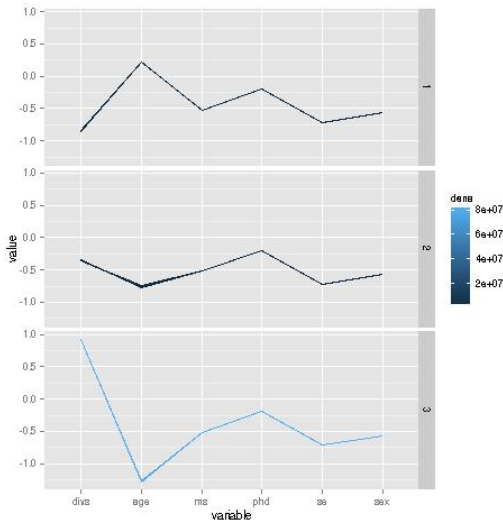
- Both R^2 values low, but nonpar. 83% higher.

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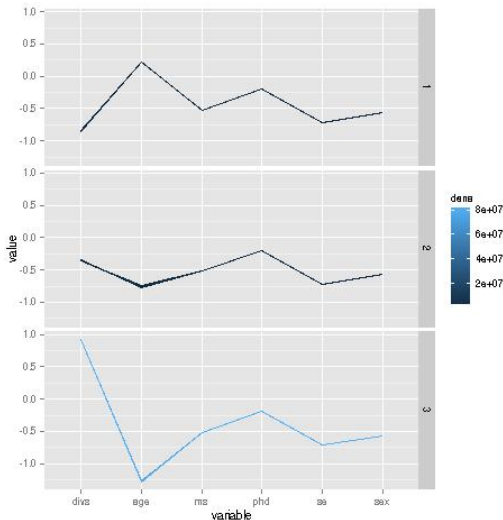
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- The Age variable seems to be the culprit: Overpredict for younger, underpredict for older.

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- This brought adj. R^2 up from 0.07 to 0.13.

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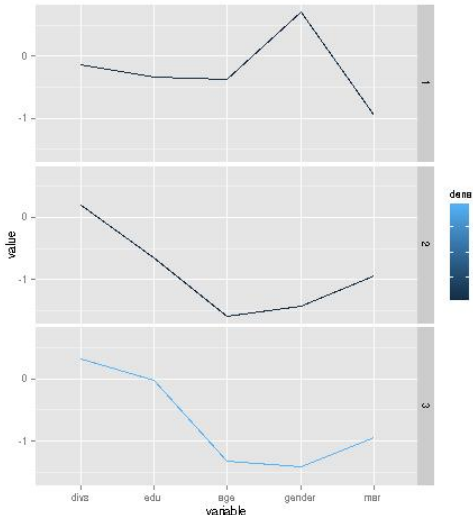
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More on Adult Data

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- Calls:

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g1 <-  
  glm(gt50 ~ edu + age + gender + mar,  
      data=newadult, family=binomial)  
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 - Did NOT improve correct-classification rate (81%).
 - BUT changed $\hat{\beta}_{Gender}$ a lot, from 0.351 to 0.610.
Interaction term -0.006. Male “advantage” in log-odds ratio now becomes, e.g. 0.46 at age 25, only 0.28 at age 55.

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- Location of these slides:
<http://heather.cs.ucdavis.edu/freqparcoord/Slides.pdf>