Norm Matloff University of California at Davis

Parallel R, Revisited

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UseR! 2012 Vanderbilt University, June, 2012

URL for these slides: http://heather.cs.ucdavis.edu/user2012.pdf (repeated on final slide)

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The Need

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The Need

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New York Times, Feb. 11, 2012

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NEWS ANALYSIS The Age of Big Data

By STEVE LOHR Published: February 11, 2012 | 🛡 82 Comments

GOOD with numbers? Fascinated by data? The sound you hear is opportunity knocking.



Mo Zhou was snapped up by I.B.M. last summer, as a freshly minted Yale M.B.A., to join the technology company's fast-growing ranks of data consultants. They help businesses make sense of an explosion of data — Web traffic and social network comments, as well as software and sensors that monitor

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SAS Web page

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SAS Web page

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Newsroom

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- Analyst Viewpoints
- About SAS
- Awards
- News: SAS Companies

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Big data: big challenges, big opportunities

An expert panel discusses how organizations can capitalize on big data to generate new ideas, build new markets and expand existing ones

Participating in a panel discussion at the recent Ideas Economy conference put on by The Economist, SAS Chief Executive Officer Jim Goodnight and other high-tech execs discussed so-called "big data" and the challenges and opportunities companies face in dealing with the ever-growing data deluge.

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Oracle Web page

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The term big data draws a lot of attention, but behind the hype there's a simple story. For decades, companies have been making business decisions based on transactional data stored in relational databases. Beyond that critical data, however, is a potential treasure trove of less structured data: weblogs, social media, email, sensors, and photographs that can be mined for useful information.

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Oracle, cont'd.

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Oracle, cont'd.

But Oracle rocks! :-)

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Oracle, cont'd.

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But Oracle rocks! :-)

Oracle R Enterprise

Integrates the Open-Source Statistical Environment R with Oracle Database 11g

Oracle R Enterprise allows analysts and statisticians to run existing R applications and use the R client directly a Oracle Database 11g—vastly increasing scalability, performance and security. The combination of Oracle Databa delivers an enterprise-ready, deeply integrated environment for advanced analytics. Users can also use analytic where they can analyze data and develop R scripts for deployment while results stay managed inside Oracle Datab

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Where Is Parallel R Today?

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- Mainly useful on "embarrassingly parallel" (EP) problems—those dividable into subproblems that need little or no intercommunication.
- What about non-EP apps?

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Challenges

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Challenges

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Parallel R, Revisited

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 - multicore

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Parallel R, Revisited

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 - cluster

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Parallel R, Revisited

- Multiplatform desirable:
 - multicore
 - cluster
 - GPU

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Parallel R, Revisited

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- GPU (and other coming accelerators?)
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- R not threaded

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- Copy-on-write:

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 - Very hard, no plans to do it to my knowledge (?).
 - **Rdsm**, **bigmemory** threads-like, but not good for parallel computation.
- Copy-on-write: Writing to one vector element sometimes causes copying entire vector.

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Challenges, cont'd.

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Challenges, cont'd.

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"When you come to a fork in the road, take it"—famous baseball player and malapropist Yogi Berra

• Parallel technology in a state of flux:

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Challenges, cont'd.

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 - OpenACC; for GPUs; might become more popular, due to announced connection with OpenMP
 - uncertainty abounds—so which way should R go?

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Outline of This Talk

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 - Rth: R interface to Thrust.
 - Thrust is C++ package for high-level operations, e.g. sort, search, prefix scan.
 - Thrust builds to multiple backends, including GPU and multicore.
 - So, Rth is a tool for easily parallelizing many R operations, usable on both GPU and multicore.

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Software Alchemy: Non-EP to EP

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• Call it NEP2EP.

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• Old, old idea in parallel processing: Break data into chunks, work on each chunk, then combine results.

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• Key point:

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Software Alchemy: Non-EP to EP

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- Old, old idea in parallel processing: Break data into chunks, work on each chunk, then combine results.
- But this requires EP to be worthwhile.
- New approach: Exploit the <u>statistical</u> properties.
- Key point: Calculate a **statistically equivalent** quantity that lends itself to EP computation.

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Advantages of NEP2EP

Norm Matloff University of California at Davis Advantages of NEP2EP

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Advantages of NEP2EP

- Works on R level; no need to resort to C/C++.
- Fine on either multicore or cluster.
- Simple to use—e.g. from snow.
- Has a surprising benefit even on unicore.
- Bonus: Automatic generation of standard errors (that you didn't have before).

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How NEP2EP Works

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How NEP2EP Works

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- Have n data points, r processes (e.g. r = 2 for dual core on a single machine).

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- Break into r chunks of n/r data points each.
- For i = 1,...,r calculate $\hat{\theta}$ on chunk i, yielding $\tilde{\theta}_i$.
- Average all those chunked values:

$$\overline{\theta} = \frac{1}{r} \sum_{i=1}^{r} \widetilde{\theta}_i$$

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R Code (Snow)

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R Code (Snow)

wrapper <- function(cls,z,probpars,sfrndmz=F) if (!is.matrix(z)) z <- matrix(z,ncol=1) n <- probpars\$n</pre> if (rndmz) z <- z[sample(1:n,n,replace=F),] nnodes <- length(cls) obslist <- list()</pre> chunksize <- n / nnodes for (i in 1:nnodes) { firstobs <-1 + (i-1) * chunksize lastobs <- firstobs + chunksize - 1 if (lastobs == n) lastobs <- n obslist [[i]] <- z[firstobs:lastobs,]</pre> } thts <- clusterApply(cls, obslist, sf) tht $\leq -$ do. call ("+", thts) tht / nnodes

Parallel R, Revisited

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What Does That Give You?

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- But the computation of $\overline{\theta}$ is EP even if $\widehat{\theta}$ is non-EP.

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What Does That Give You?

- The result, $\overline{\theta}$ can be proven to have the same asymp. statistical accuracy as the original $\widehat{\theta}$.
- But the computation of $\overline{\theta}$ is EP even if $\widehat{\theta}$ is non-EP.
- Alchemy! Non-EP \rightarrow EP.

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Rough Theoretical Speedup Analysis

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- For algs. having c > 1, speedup is *superlinear* (par. proc. term).

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- For algs. having c > 1, speedup is *superlinear* (par. proc. term).Not the usual small stuff like cache effects!

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Rough Theoretical Speedup Analysis

- Say n obs., r processes (e.g. r = 2 for dual core).
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• Uniprocessing case: Run time is $rO(n^c/r^c)$, i.e. $O(n^c/r^{c-1})$.

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- Uniprocessing case: Run time is $rO(n^c/r^c)$, i.e. $O(n^c/r^{c-1})$. So, if c > 1 NEP2EP gives a speedup with no parallelism!

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NEP2EP Timing Experiments

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NEP2EP Timing Experiments

NEP2EP in Snow

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NEP2EP Timing Experiments

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- NEP2EP in Snow
- multicore machine, 32 threads (2 CPUs x 8 cores x hyperthreading of 2)

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NEP2EP Timing Experiments

- NEP2EP in Snow
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- num. cores = 2,4,8,16,24,32;

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NEP2EP Timing Experiments

- NEP2EP in Snow
- multicore machine, 32 threads (2 CPUs x 8 cores x hyperthreading of 2)
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NEP2EP Timing Experiments

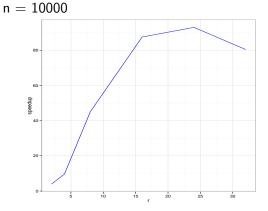
- NEP2EP in Snow
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- num. cores = 2,4,8,16,24,32; sometimes better beyond 32, probably due to cache/VM effects

- procedures tried:
 - Kendall's au
 - quantile regression
 - nonparametric hazard function est.
 - log-concave density est.
 - linear regression (random x)

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Kendall's τ

Kendall's τ



3.92X speedup at 2 threads 93.97X speedup at 24 threads

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Parallel R, Revisited

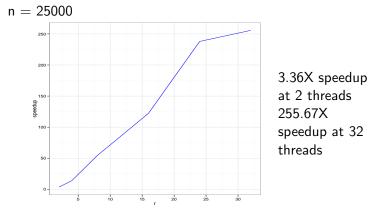
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Kendall's τ , cont'd.

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Kendall's τ , cont'd.



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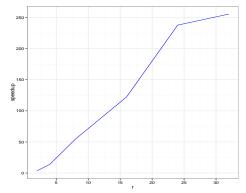
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Quantile Regression

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Quantile Regression

 $n = 10000, \, p = 10$



0.86X speedup at 2 threads 1.16X speedup at 8 threads

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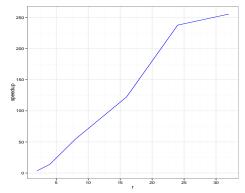
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Quantile Regression

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Quantile Regression

n = 10000, p = 25



3.36X speedup at 2 threads 255.67X speedup at 32 threads

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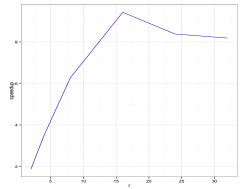
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Hazard Function Estimation

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Hazard Function Estimation

 $n=25000,\,p=0.2$ (proportion missing); estimate quantiles 0.2, 0.4, 0.6, 0.8



1.87X speedup at 2 threads 9.43X speedup at 16 threads

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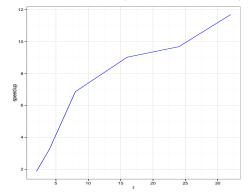
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Hazard Function Estimation

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Hazard Function Estimation

n = 50000, p = 0.02 (proportion missing)



1.87X speedup at 2 threads 11.69X speedup at 32 threads

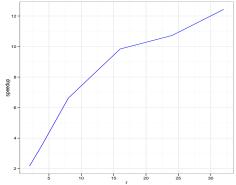
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Log Concave Density Estimation

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Log Concave Density Estimation

n = 200000



2.17X speedup at 2 threads 12.43X speedup at 32 threads

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Linear Regression

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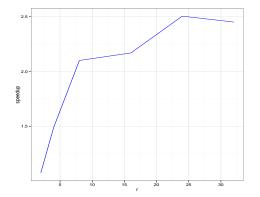
Linear Regression

n = 50000, p = 50; should expect less here, $O(n, p^3)$

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Linear Regression

n = 50000, p = 50; should expect less here, $O(n, p^3)$



0.90X speedup at 2 threads 1.97X speedup at 32 threads

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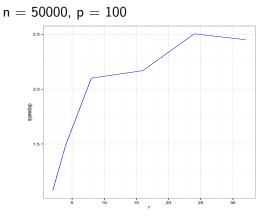
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Linear Regression

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Linear Regression

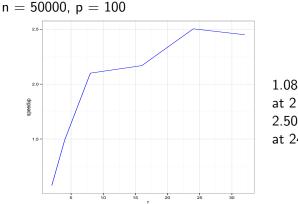


1.08X speedup at 2 threads 2.50X speedup at 24 threads

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Linear Regression



1.08X speedup at 2 threads 2.50X speedup at 24 threads

Put in context: Seligman (2010) found GPU provides speedup only if $\mathsf{r}>1000.$

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What About the Large-Sample Nature?

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What About the Large-Sample Nature?

• One can prove that NEP2EP works <u>asymptotically</u>, i.e. gives the same statistical accuracy as the original estimatator.

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What About the Large-Sample Nature?

• One can prove that NEP2EP works <u>asymptotically</u>, i.e. gives the same statistical accuracy as the original estimatator. Is that large-n requirement an issue?

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• No, not an issue:

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What About the Large-Sample Nature?

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- No, not an issue: Since we're talking about settings where parallel computing is needed, we're working with large samples by definition

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What About the Large-Sample Nature?

- One can prove that NEP2EP works <u>asymptotically</u>, i.e. gives the same statistical accuracy as the original estimatator. Is that large-n requirement an issue?
- No, not an issue: Since we're talking about settings where parallel computing is needed, we're working with large samples by definition—the large n is the reason we need parallel computing!
- NEP2EP gives essentially the same values as the original.

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Accuracy

Absolute differences, r = 16:

Accuracy

Parallel R, Revisited

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Absolute differences, r = 16:

app.	prob. size	rel. diff.
Kendall	n = 1000	0.005849463
quant. reg.	n = 10000, p = 10	0.001274819
haz. ftn.	n = 25000, p = 0.2	0.007422595
log conc. dens.	n = 25000	0.0003593208
lin. reg.	n = 50000, p = 100	0.0001207394

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Rth

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Rth

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Motivations:

• Parallelizing R will need to rely in part on C/C++ code.

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Rth

- Parallelizing R will need to rely in part on C/C++ code.
- Nice to have the same parallel code work on multicore and GPU systems.

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Rth

- Parallelizing R will need to rely in part on $C/C{++}\xspace$ code.
- Nice to have the same parallel code work on multicore and GPU systems. PGP—Pretty Good Parallelism.

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Rth

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- Nice to have code for high-level operations available (sort, search, prefix scan, etc.).

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Rth

- Parallelizing R will need to rely in part on C/C++ code.
- Nice to have the same parallel code work on multicore and GPU systems. PGP—Pretty Good Parallelism.
- Nice to have code for high-level operations available (sort, search, prefix scan, etc.).
- Hopefully make it (somewhat) easy for users to write their own parallel code.

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Some Existing Possibilities

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Some Existing Possibilities

These work on both multicore and GPUs:

- OpenCL: Extension of C.
- Magma: Matrix routines.
- OpenACC: Like OpenMP for GPUs.

But OpenCL and OpenACC do not provide high-level ops, and Magma is narrow.

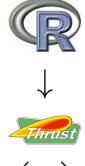
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Rth

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Rth









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Goals

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Goals

• Provide parallel Thrust code called from R,

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Goals

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- Provide parallel Thrust code called from R,
- Thrust transparent to the ordinary user.

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Goals

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- Provide parallel Thrust code called from R,
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- Parallelize a number of R operations in Thrust.

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Goals

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- Provide parallel Thrust code called from R,
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- Parallelize a number of R operations in Thrust.
- Facilitate sophisticated user writing own parallel code.

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Goals

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- Provide parallel Thrust code called from R,
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- Facilitate sophisticated user writing own parallel code.
- Currently just at very early stage of project.

What is Thrust?

Goals

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Parallel R, Revisited

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What is Thrust?

• C++ package, modeled on STL.

Goals

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- Parallel R, Revisited
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- Facilitate sophisticated user writing own parallel code.
- Currently just at very early stage of project.

What is Thrust?

- C++ package, modeled on STL.
- Can compile to either GPU or multicore backend.
- Provides high-level operations, e.g. sort, search, prefix scan, foreach, reduction, etc.

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Example: sorting

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Example: sorting

R interface code:

```
rthsort <- function(x) {
   dyn.load("rthsort.so")
   n <- length(x)
   tmp <- .C("rthsort",as.double(x),
        as.integer(n),tmpres=double(n))
   return(tmp$tmpres)
}</pre>
```

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Example: sorting

```
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```

Sorting 10000000 numbers: R 4.78 sec, Rth 1.52sec.

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sorting, cont'd.

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sorting, cont'd.

Thrust code:

```
#include <thrust/host_vector.h>
#include <thrust/device_vector.h>
#include <thrust/sort.h>
```

```
void rthsort(double *x, int *nx, double *xout)
{
    int n = *nx;
    // set up device vector and copy x to it
    thrust::device_vector<double> dx(x,x+n);
    // sort, then copy back to x
    thrust::sort(dx.begin(), dx.end());
    thrust::copy(dx.begin(), dx.end(),xout);
}
```

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General Pattern

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General Pattern

Sort example was straight wrapper. What about other cases?

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General Pattern

Sort example was straight wrapper. What about other cases?

• Put together the appropriate Thrust ops.

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General Pattern

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Sort example was straight wrapper. What about other cases?

- Put together the appropriate Thrust ops.
- For most Thrust ops, write app-specific function to be called.

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Example: convolution

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Thrust code:

Example: convolution

void rthconv(double *x, int *nx, double *y, int *ny, double *z) { int nxx = *nx, nyy = *ny, nzz = nxx + nyy thrust :: device_vector <double> dx(x, x+nxx); . . . thrust :: counting_iterator <int> seqb(0); thrust :: counting_iterator <int> seqe = seqb thrust :: for_each (seqb, seqe, doli(dx.begin(), dy.begin(),dz.begin(),nxx,nyy)); thrust :: copy(dz.begin(), dz.end(),z); } Key line:

thrust :: for_each (seqb, seqe, do1i(dx.begin(),...

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convolution, cont'd.

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convolution, cont'd.

```
User supplies "foreach" function, in the form of a
struct doli { // "do 1 i"
. . .
   device
   void operator()(const int i)
   { int j; // handle 1 i in i, j loop
      int rpi = rndperm[i];
      double xdi = xd[rpi];
      for (j = 0; j < ny; j++)
         zd[rpi+j] += xdi * yd[ny-j-1];
   }
};
```

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convolution, cont'd.

```
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. . .
   device
   void operator()(const int i)
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      double xdi = xd[rpi];
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         zd[rpi+j] += xdi * yd[ny-j-1];
   }
};
```

A callable struct.

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Performance

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Performance

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Performance

• Rth's rthconv() orders of magnitude faster than R's convolve().

Performance

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- Rth's rthconv() orders of magnitude faster than R's convolve().
- Not fair to R's convolve();

Performance

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Parallel R, Revisited

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- Rth's rthconv() orders of magnitude faster than R's convolve().
- Not fair to R's **convolve()**; latter written in C, but works via FFTs, slow.

Performance

- Rth's rthconv() orders of magnitude faster than R's convolve().
- Not fair to R's **convolve()**; latter written in C, but works via FFTs, slow.
- Also: R's **convolve()** runs out of space on problems than **rthconv()** can handle (multcore).

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Parallel R, Revisited

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Kendall's Tau

Kendall's Tau

```
void rthkendall(float *xy, int *nxy, float *tau)
  int i, n = *nxy, n2 = 2*n, totcount;
  thrust :: counting_iterator < int > seqa(0);
  thrust :: counting_iterator <int>
    seqb = seqa + n - 1;
  doubvec dxy(xy, xy+n2);
  intvec tmp(n-1);
  thrust :: transform (seqa, seqb, tmp. begin (),
    calcgti(dxy,n));
  totcount=thrust :: reduce(tmp.begin(),tmp.end(
  *tau = totcount / (0.5 * n * (n-1));
}
```

Key calls: **transform(), reduce()**; can combine using transform iterator

Parallel R, Revisited

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Example: submatrix ops, select()

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Example: submatrix ops, select()

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• Not implemented yet.

Norm Matloff University of California at Davis Example: submatrix ops, select()

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- Not implemented yet.
- Easy version: Specific numerical indices.

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Example: submatrix ops, select()

- Not implemented yet.
- Easy version: Specific numerical indices.
- More elaborate: Dynamic parse of user R expression, sent off to Thrust code.

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Some Thrust Ops

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Some Thrust Ops

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- sort, search
- reduce, min/max
- permute (e.g. for matrix transpose)
- partition, prefix scan
- foreach, transform, copyif
- set ops
- more are being added

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• "Software alchemy" parallelizes i.i.d. stat apps, any platform.

Summary

Parallel R, Revisited

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• "Software alchemy" parallelizes i.i.d. stat apps, any platform. Often get superlinear speedup.

Summary

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- "Software alchemy" parallelizes i.i.d. stat apps, any platform. Often get superlinear speedup.
- Rth provides a way to easily parallelize many other opps.

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Misc.

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Misc.

Parallel R, Revisited

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URLs:

• these slides:

http://heather.cs.ucdavis.edu/user2012.pdf

- my online book on parallel programming: http://heather.cs.ucdavis.edu/~matloff/158/ PLN/ParProcBook.pdf
- Rth: http:

//heather.cs.ucdavis.edu/~matloff/rth.html

thanks to:

- Prof. Hao Chen (use of large multcore machine)
- Prof. Bill Hsu (use of fast GPUs)
- the audience :-)