Parallel Coordinates—REVISITED

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(new collaborator: Yingkang Xie)

Bay Area R Users Group
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Outline

• What IS parallel coordinates, anyway?
• SEEMS to be a great tool. But has MAJOR problems.
• I will present a novel way to make parallel coordinates usable.
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What IS Parallel Coordinates?

• Attempt to view multidimensional data on 2-dimensional screen.
• Simple idea:
  • Draw a vertical line for each variable ("parallel coords.").
  • For each data point, mark a dot on each vertical line, at the value of that variable for that data point.
  • For each data point, "connect the dots."
  • Resulting graph: a jagged line for each of your original data point.
• Can then try to find relations between variables by looking at line patterns.
• The operative word is "try."
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- Note: Variables are typically centered and scaled.
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Problems

Hard to interpret, except in "small n, small p" data. (p = number of variables)

Problem 1: Hard to see relation between "far apart" variables

Typical solution:
Allow user to interactively do various permutations of the axes.

Problem 2: Screen clutter!!!!

Typical solutions:
1. $\alpha$ blending (making pixels less dark).
2. Plotting line density instead of lines (equiv. to tonal, like $\alpha$).
3. Look at random subset of the data.
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Example: Baseball Player data—height, weight, age (courtesy of UCLA Stat. Dept.)
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Another Example of Clutter
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Example: Wine Quality data—various chemical measures (UCI Repository)
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Alpha Blending May Not Help Much
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Yikes!

Comments:

• Yikes!
• “Don’t let the picture intimidate you!”—A. Inselberg, one of the pioneers of parallel coordinates, speaking in general of cluttered p.c. plots
• But it IS intimidating!
• Can TRY to exploit geometric properties:
  • X shape ⇒ negative ρ
  • < shape ⇒ positive ρ
  • Nice theory, form projective geometry, etc.
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Example of Clutter, cont’d.
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Grouping by player position doesn’t help much:
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Variables are chemical measures, plus a quality variable.
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Need domain expert to interpret, but distinction between quality groups is clear.
How Many to Plot?

We plot "a few of the most typical lines."

• My software asks the user to define "a few," in an argument m.

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• m larger ⇒ better chance to see ρ's among the most typical data points.
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- \( m \) larger \( \Rightarrow \) better chance to see \( \rho \)’s among the most typical data points
More Features

• Cluster hunting. Instead of finding global max of density, plot jagged line at each local maximum
• Outlier hunting. Plot the least typical lines.
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- Use R’s FNN ("fast nearest neighbor") library for some speed.
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- Use R’s FNN (“fast nearest neighbor”) library for some speed.
- Use parallel computing for a lot more speed.